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Taro TAKAGUCHI, Mitsuhiro NAKAMURA, Nobuo SATO, Kazuo YANO, and Naoki MASUDA

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Abstract

Recent developments in sensing technologies have enabled us to examine the nature of human social behavior in greater detail. By applying an information theoretic method to the spatiotemporal data of cell-phone locations, Song et al. (2010) found that human mobility patterns are remarkably predictable. Inspired by their work, we address a similar predictability question in a different kind of human social activity: conversation events. The predictability in the sequence of one's conversation partners is defined as the degree to which one's next conversation partner can be predicted given the current partner. We quantify this predictability by using the mutual information. We examine the predictability of conversation events for each individual using the longitudinal data of face-to-face interactions collected from two company offices in Japan. Each subject wears a name tag equipped with an infrared sensor node, and conversation events are marked when signals are exchanged between close sensor nodes. We find that the conversation events are predictable to some extent; knowing the current partner decreases the uncertainty about the next partner by 28.4% on average. Much of the predictability is explained by long-tailed distributions of inter-event intervals. However, an indigenous predictability also exists in the data, apart from the contribution of their long-tailed nature. In addition, an individual's predictability is correlated with the position in the static social network derived from the data. Individuals confined in a community in the sense of an abundance of surrounding triangles tend to have low predictability, and those bridging different communities tend to have high predictability.

1 Introduction

In recent times, interest in the statistical and dynamical features of human social behavior has been growing, supplemented by the development of new devices that enables tracking of social data in real time with increasing precision and duration [1–9]. A recent remarkable finding from the analysis of spatiotemporal data of cell-phone locations is that human mobility patterns are highly predictable [2, 10, 11], a finding that is in contrast to the classical view. For instance, in epidemic models that take the mobility of subjects into account, subjects are usually assumed to perform a conventional random walk from one location to another [12, 13]. However, actual traveling patterns of humans often deviate from such random walk models, and the displacement distribution follows the power law [2, 14]. Furthermore, the statistics of the next location of the individual is affected by not only the current location but also the history of the traveling pattern, resulting in approximately 90% predictability of the mobility patterns [10].

In this study, we address a similar predictability question for a different component of human social behavior: conversation events. Conversation events mediate spreading and routing of diverse contents such as new ideas, opinions, and infectious diseases in social networks [15, 16]. In models describing these phenomena, it is a norm that each individual possesses a dynamically changing state (*e.g.*, opinion A or opinion B in opinion dynamics, and susceptible or infected state in epidemic dynamics). The law of transition from one state to another is usually assumed to be Markovian, *i.e.*, independent of the history of the process. The Markovian property, which is a type of unpredictability, is a null assumption for simulating such dynamics based on a static social network [15, 16].

However, the plausibility of this null assumption is unclear. Imagine the office that you share with other colleagues in a company. When you have a question about a project, you may talk to your boss. After this conversation event, you may tend to talk to a particular individual to communicate the instruction of the boss. During lunchtime, you may chat with your close colleagues in a particular order that you do not perceive. How predictable is your choice of your next conversation partner given the current partner?

We examine the predictability of conversation events using two sets of longitudinal data collected from company offices in Japan. Our data are unique in that they are collected from a relatively high number of individuals (*i.e.*, approximately 200 individuals) over a long recording period (*i.e.*, approximately three months). We adopt an ego-centric network view to examine the sequence of conversation events for each individual. We find that a conversation event has notable deterministic components. In other words, the uncertainty about the next partner that you talk with decreases by 28.4% on average, given the identity of the partner you are currently talking with (see Sec. 3.2).

It should be noted that our approach is related to but different from the studies of power-law interval distributions in conversation events. The interval between successive conversation events for an individual or a given pair of individuals often follows a power law [1,4–6,8,17–20]. Modeling studies have revealed implications of these empirical results in contagions [4, 6, 9, 21–25] and opinion formation [26, 27]. In contrast to conventional models in which the Poisson interval distribution is assumed, these results indicate that the next conversation time given the previous one is relatively predictable in that a conversation event in the recent past is a precursor to a burst of events in the near future. We argue that this bursty nature of the point process largely contributes to the predictability of conversation events.

We also show that the degree of predictability depends on individuals. Individuals located inside a network community, *i.e.*, a dense subnetwork loosely connected to other parts of the entire network [28], quantified in this study via strong links and the clustering coefficient, behave relatively randomly. On the other hand, individuals that connect different communities by weak links tend to have a high predictability.

2 Data and Methods

We analyze two sets of face-to-face interaction logs obtained from different company offices using the Business Microscope system developed by Hitachi, Ltd., Japan [29, 30]. Data set D_1 consists of recordings from N = 163 individuals for 73 days. Data set D_2 consists of recordings from N = 211individuals for 120 days. Each subject wears a name tag strapped around the neck and placed at the chest, and each name tag contains an infrared module. The infrared modules can communicate with each other if they are less than three meters apart. An infrared module only senses the modules situated within a 120° circular sector in front of the name tag, and the system detects conversation events only when two individuals are facing each other. Communication between modules includes exchanging the owners' IDs every 10 seconds. We regard two individuals to be involved in a conversation event if their infrared modules communicate with each other at least once in a minute. In other words, the time resolution of the system is equal to one minute. The list of conversation partners and time stamps is stored in the name tag of each individual and sent to the central database on a daily basis. The data transfer occurs when the individual leaves work and put the name tag on the gateway device connected to the individual's computer [29, 30]. Each data set contains a list of conversation events, as shown in Fig. 1. A conversation event is specified by the IDs of the two individuals talking with each other, the date and time at which the dialogue starts, and the duration of the dialogue. We are not concerned with the content of the dialogue. Data sets D_1 and D_2 contain 51,879 and 125,345 events, respectively.

We investigate the predictability of each individual's conversation patterns. Our preliminary data analysis revealed that the timing of conversation events lacks sufficient temporal correlation and is unpredictable. Therefore, we neglect the timing of conversation events in the data unless otherwise stated and focus on the partner sequence defined as follows. To generate the partner sequence of individual 1, we first sift out all the conversation events that involve individual 1 from the entire data set (Fig. 1(b)). Next, we ignore the time stamp and duration of the conversation events. The remaining data define the partner sequence, *i.e.*, the chronologically ordered sequence of the IDs of the conversation partners for individual 1 (Fig. 1(c)). When multiple conversation events involving individual 1 are initiated in the same minute, we determine their order at random.

To evaluate the predictability of the partner sequence, we calculate three entropy measures, inspired by those used for the analysis of human mobility patterns [10]. First, we define the random entropy for individual i as

$$H_i^0 \equiv \log_2 k_i,\tag{1}$$

where k_i represents the number of *i*'s partners for the entire recording. If *i* chooses the partner with equal probability $1/k_i$ from all the *i*'s acquaintances in each conversation event, H_i^0 quantifies the degree of randomness. Second, we define the uncorrelated entropy as

$$H_i^1 \equiv -\sum_{j \in \mathcal{N}_i} \mathcal{P}_i(j) \log_2 \mathcal{P}_i(j), \tag{2}$$

where \mathcal{N}_i is the set of *i*'s partners containing k_i elements. $P_i(j)$ represents the probability that individual *i* talks with individual *j* in a conversation event for *i*; the normalization is given by $\sum_{j \in \mathcal{N}_i} P_i(j) = 1$. As compared to H_i^0 , H_i^1 accounts for the heterogeneity among $P_i(j)$ $(j \neq i)$. Third, we define the conditional entropy as

$$H_i^2 \equiv -\sum_{j \in \mathcal{N}_i} \mathcal{P}_i(j) \sum_{\ell \in \mathcal{N}_i} \mathcal{P}_i(\ell|j) \log_2 \mathcal{P}_i(\ell|j),$$
(3)

where $P_i(\ell|j)$ represents the conditional probability that individual *i* talks with individual ℓ immediately after talking with individual *j*. H_i^2 measures the second-order correlation in the partner sequence of *i*. For each individual, $0 \le H_i^2 \le H_i^1 \le H_i^0$ is satisfied. We quantify the predictability of the partner

sequence by the mutual information as follows:

$$I_i \equiv H_i^1 - H_i^2 = \sum_{j,\ell \in \mathcal{N}_i} \mathcal{P}_i(\ell,j) \log_2 \frac{\mathcal{P}_i(\ell,j)}{\mathcal{P}_i(\ell)\mathcal{P}_i(j)},\tag{4}$$

where $P_i(\ell, j)$ represents the joint probability that individual *i* talks with individual ℓ immediately after talking with individual *j*. For each individual, $0 \leq I_i \leq H_i^1$ is satisfied. I_i quantifies the predictability of the partner sequence; it is equal to the amount of the information about the next partner that is earned by knowing the current partner. When the partner sequence lacks a second-order correlation such that $H_i^1 = H_i^2$, I_i takes the minimum value 0. In this case, knowing the current partner does not help predict the next partner at all. When the partner sequence is completely deterministic, *i.e.*, the next partner is completely predicted from the current partner such that $H_i^2 = 0$, I_i takes the maximum value H_i^1 .

Although our prime interest in this study is the temporal properties of partner sequences, we also analyze the conversation networks (CNs) G_1 and G_2 constructed by aggregating all the conversation events in D_1 and D_2 , respectively, over the entire recording. In a CN, the node represents an individual, and the weight of the link, denoted as w_{ij} , represents the number of conversation events between individuals *i* and *j* during the entire recording period. By the definition of the conversation event, $w_{ij} = w_{ji}$ ($i, j = 1, 2, \dots, N$) holds true; the CN is an undirected network. The degree k_i of individual *i* is equal to the number of *js* for which $w_{ij} > 0$.

3 Results

3.1 Properties of the CN

We found that both CNs, G_1 and G_2 , are composed of a single connected component. The CN G_1 is visualized in Fig. 2; we will analyze the relation between the CNs and the predictability in Sec. 3.3. The clustering coefficient [31] of the unweighted versions of G_1 and G_2 is equal to 0.646 and 0.611, respectively. The Pearson assortativity coefficient [32] of G_1 and G_2 is equal to 0.169 and 0.296, respectively. Therefore, the CNs have typical properties of social networks [33], *i.e.*, high clustering and positive assortativity.

For the two CNs, we measure the distributions of degree, node strength, and link weight. The node strength s_i is the sum of link weights connecting to node i [34, 35], *i.e.*, the total number of conversation events for individual i, defined as

$$s_i \equiv \sum_{j \in \mathcal{N}_i} w_{ij}.$$
 (5)

The mean and standard deviation of k_i of G_1 and G_2 are equal to 26.07 ± 11.01 and 69.56 ± 29.47 (mean \pm standard deviation), respectively. Because two individuals are adjacent if there is at least one conversation event for a few months, the mean k_i of both networks is relatively large. s_i of G_1 and G_2 is equal to 636.6 ± 516.7 and 1188.1 ± 622.1 , respectively. w_{ij} of G_1 and G_2 is equal to 24.41 ± 53.69 and 17.08 ± 45.77 , respectively. The cumulative distribution of the three quantities are shown in Fig. 3.

3.2 Predictability of partner sequences

We examine the predictability of partner sequences using the entropy measures. Because the estimation of entropy is notoriously biased when the data size is small, we discard individuals with less than 100 conversation events (*i.e.*, $s_i < 100$). There remain 146 and 210 individuals in data sets D_1 and D_2 , respectively after the thresholding. Because the results for the two datasets are similar, we report the results for D_1 in the following. The results for D_2 are given in Appendix A.

The histograms of the three types of entropies for partner sequences are shown in Fig. 4(a). For all the individuals, H_i^1 is at least 9.94% smaller than H_i^0 . This implies that individuals preferentially select particular partners from their neighbors in the CN.

The values of H_i^1 and H_i^2 for each individual are shown in Fig. 4(b). The mutual information $I_i = H_i^1 - H_i^2$ is positive for all the individuals regardless of the value of H_i^1 . In general, the finite size effect decreases H_i^1 and H_i^2 by different amounts such that the estimated I_i is generally inherited with a positive bias [36]. For our data, the positive values of I_i are not an artifact caused by the small data size. Through a bootstrap test (see Appendix B for details), we confirmed that the empirical values of I_i are significantly (at 1% level) larger than the values obtained from the bootstrap samples. In short, the bootstrap samples are randomized partner sequences that destroy temporal correlation in the data but preserve the original H_i^1 and account for the portion of I_i derived from the finite size effect. It should also be noted that we determined the order of partners at random when conversation events with different partners initiate in the same minute. This randomization does not make I_i larger because it conserves H_i^1 and the fraction of such overlapping conversation events for individual i ($1 \leq i \leq N$, $s_i \geq 100$) is slightly negative (*i.e.*, -0.0811). In summary, the information about the current conversation partner gives the information about the next partner; H_i^2 is, on average, 28.4% smaller than H_i^1 .

The predictability present in the data is mainly explained by the bursty activity patterns, *i.e.*, long-tailed distributions of the inter-event intervals, which have been observed for various data [1, 4-6, 8, 17-20]. Our data also possess this feature (see Appendix C for details). Because the inter-event interval for a given pair of individuals obeys a long-tailed distribution, individual *i* tends to talk with individual *j* within a short period after talking with *j*. In the remainder of this section, we show that the predictability is mainly caused by the bursty activity patterns (Fig. 5(a)) and that the predictability still remains even if we omit the contribution of the burstiness from the partner sequence (Fig. 5(b)).

We examine the contribution of the bursty activity pattern to the predictability by calculating the mutual information I_i^{burst} of the randomized partner sequence. The randomization of the inter-event intervals between each pair of individuals is realized by swapping inter-event intervals of the original data within each day in a completely random order (see Appendix D for the precise methods). Due to the computational cost of the randomization procedure, we obtain the mean and standard deviation of I_i^{burst} from 100 randomized partner sequences, instead of estimating the confidential interval of I_i^{burst} . The mean I_i^{burst} accounts for 79.5% of the original I_i on an average (Fig. 5(a)). Because the randomization procedure preserves the inter-event interval distribution, Fig. 5(a) suggests that a large I_i is mainly attributed to the bursty activity patterns. It should be noted that I_i^{burst} is large partly because the randomizing procedure conserves the timings of the first and last conversation events of each pair on any day. Therefore, we may be overestimating the contribution of burstiness to I_i .

The predictability is not solely determined by the bursty activity patterns. To clarify this point, we calculate the mutual information I_i^{merge} of the modified partner sequence generated by merging the consecutive conversation events with the same partner in the original partner sequence into one event. This merging procedure allows us to eliminate the contribution of the bursty activity pattern to the predictability. For example, if individual *i* talks with individual *j* three times without being interrupted by other partners, we merge the three conversation events into one. The values of I_i^{merge} are shown in Fig. 5(b). To confirm that the positive values of I_i^{merge} are not an artifact caused by the small data size, we carry out a bootstrap test for I_i^{merge} similar to that for I_i . By definition, no partner ID appears successively in the merged partner sequence. Therefore, we generate the bootstrap sample of the merged partner sequence by sampling from the merged sequence with replacement under the condition that the same partner is not consecutively chosen (see Appendix D for details). I_i^{merge} is significantly larger than the values obtained from the bootstrap samples. Therefore, the original partner sequence possesses some predictability even after removing bursts originating from the bursty nature.

3.3 Variation among the predictabilities of individuals

The predictability, quantified by I_i , depends on individuals. In this section, we investigate the relationship between the predictability of individuals and properties of nodes in the CN. The results shown in this section are summarized as follows. First, I_i is negatively correlated with node strength s_i and with mean node weight defined as $\overline{w}_i \equiv \sum_{j \in \mathcal{N}_i} w_{ij}/k_i$ (Fig. 6). Second, the CN possesses the "strength of weak ties" structure (Fig. 7(a)). Third, the individuals bridging different communities with weak links tend to have large I_i , and those concealed in a single community and surrounded by strong links tend to have small I_i (Fig. 7(b)).

One may speculate that I_i is strongly affected by the node degree k_i because $H_i^0 = \log_2 k_i$ and H_i^1 and H_i^2 comprise many terms if k_i is large. However, k_i and I_i are uncorrelated, as shown in Fig. 6(a). We found that I_i is negatively correlated with s_i (Fig. 6(b)) and with \overline{w}_i (Fig. 6(c)). We verified using the bootstrap test that the negative correlation shown in Fig. 6(b) and 6(c) is not because of the finite sampling size (see Appendix B for details). The correlation shown in Fig. 6 and the following results do not qualitatively change if we use the normalized mutual information [37] I_i/H_i^1 (see Appendix E). We also verified that alternatively defining the link weight by the total duration of the conversation events for each pair, instead of the total number of the conversation events, does not qualitatively change the results described in this section (see Appendix F for details).

For a fixed k_i , both s_i and \overline{w}_i decrease with the number of weak links (*i.e.*, the links with small weight) connected to individual *i*. This fact leads us to hypothesize that individuals surrounded by weak links select partners in a relatively deterministic order. According to Granovetter's theory of the strength of weak ties, weak links tend to interconnect different communities in a social network and bring valuable external information to both end nodes, while strong links tend to be intracommunity links [38]. Therefore, the individuals bridging different communities with weak links may have large values of I_i .

We first verify the "strength of weak ties" hypothesis in the CN. The network visualized in Fig. 2 appears to be consistent with the hypothesis; weak links tend to connect communities composed of strong links. To quantify the extent to which a link is engaged in intracommunity connection, we

measure the relative neighborhood overlap of a link [39], defined as

$$O_{ij} = \frac{|\mathcal{N}_i \cap \mathcal{N}_j|}{|\mathcal{N}_i \cup \mathcal{N}_j| - 2},\tag{6}$$

where $|\cdot|$ denotes the number of elements in the set. When $O_{ij} = 0$, individuals *i* and *j* do not have a common neighbor and the link (i, j) is considered to connect different communities. When $O_{ij} = 1$, individuals *i* and *j* share all of the neighbors and the link (i, j) is confined in a community. The "strength of weak ties" hypothesis suggests that O_{ij} is positively correlated with w_{ij} [39]. In Fig. 7(a), O_{ij} averaged over the links with weights smaller than *w*, denoted as $\langle O \rangle_w$, is plotted against the fraction of links with weights smaller than *w*, denoted as $P_{cum}(w)$. Because $\langle O \rangle_w$ monotonically increases with $P_{cum}(w)$, the CN possesses the "strength of weak ties" property, as in the case of mobile communication networks [39].

Because weak links are associated with a large I_i (Fig. 6(c)) and intercommunity links (Fig. 7(a)), individuals with a large I_i are expected to bridge different communities and those with a small I_i are expected to be shielded inside a community. This concept is consistent with the visual inspection of Fig. 2. To verify this point, we show that I_i is negatively correlated with a calibrated clustering coefficient in the following (Fig. 7(b)). Note that, when the clustering coefficient is large, the individual tends to be inside a community quantified by the abundance of triangles [40]. When it is small, the individual tends to connect different communities [41, 42].

The clustering coefficient for each node is defined by $C_i =$ (number of triangles including individual i)/ $[k_i(k_i-1)/2]$ ($0 \le C_i \le 1, i=1,2,\cdots,N$) [31]. In Fig. 7(b), the Pearson correlation coefficient between I_i and $C_i(w_{\text{thr}})$ is plotted against w_{thr} , where $C_i(w_{\text{thr}})$ is the local clustering coefficient C_i for the subgraph of the CN generated by eliminating the links with weights smaller than $w_{\rm thr}$. We opted to use $C_i(w_{\rm thr})$ instead of the weighted clustering coefficient defined for weighted networks [35, 43] because the latter quantity is, by definition, strongly correlated with s_i and \overline{w}_i ; we already discussed the negative correlation between I_i and s_i and between I_i and \overline{w}_i in Fig. 6(b) and 6(c), respectively. For $w_{\rm thr} = 1$, I_i and $C_i(w_{\rm thr})$ are almost uncorrelated. This is because almost all the individuals have a large C_i regardless of I_i in the original CN G_1 (refer to Fig. 2 for a visual confirmation of this statement). For $2 \le w_{\text{thr}} \le 100$, I_i and $C_i(w_{\text{thr}})$ are negatively correlated (squares in Fig. 7(b)). Therefore, an individual with a large I_i tends to bridge different communities as quantified by the clustering coefficient. An individual with a small I_i tends to be confined within communities. The circles in Fig. 7(b) represent the partial correlation coefficient between I_i and $C_i(w_{\text{thr}})$, with $k_i(w_{\text{thr}})$ and $s_i(w_{\text{thr}})$ fixed. Here, $k_i(w_{\text{thr}})$ and $s_i(w_{\text{thr}})$ are, respectively, the degree and strength of individual i, calculated after eliminating the links with weights smaller than $w_{\rm thr}$. Because the Pearson and partial correlation coefficients behave similarly, the negative correlation between I_i and $C_i(w_{\text{thr}})$ is not ascribed to the negative correlation between I_i and s_i (Fig. 6(b)) or between I_i and \overline{w}_i (Fig. 6(c)).

In the closing of this section, we remark the robustness of our results against observation failures. The wearable tag used in our measurement fails to detect a conversation event if the tag is sealed behind obstacles such as a desk or partition. For example, suppose that two individuals chat for five minutes and either of their tags is just under a desk and is undetected in the third minute. Then, the single conversation event is split into two spurious conversation events, each lasting for two minutes. To examine the robustness of our results against such observation failures, we repeat the same set of analysis after filling short intervals between successive conversations between the same pair of individuals. If individual i has two successive conversation events with individual j and the

interval between the two events is smaller than m minutes, we merge the two events into one. The original partner sequence corresponds to m = 0. The number of conversation events decreases with m. The interpolation reduces w_{ij} , s_i , and \overline{w}_i and conserves k_i , H_i^0 , and C_i . We confirmed that our findings are reproduced when we interpolate the original data with m = 1 and m = 5 (see Appendix G for details).

4 Discussion

We have shown that sequences of conversation events have deterministic components. The entropy in the distribution of the conversation partner of an individual decreases by, on an average, 28.4% for data set D_1 and 34.8% for data set D_2 , if we know the current partner. Much of the predictability of conversation events results from the bursty activity patterns. In general, daily and weekly rhythms of human activity can cause bursty activity patterns [20]. During the night and weekend, the individuals are out of the office. Therefore, inter-event intervals are usually longer than those within working hours. Nevertheless, we consider that the effects of such long inter-event intervals on the predictability of conversation partners is small. This is because the fraction of long inter-event intervals, *i.e.*, those over five hours, for example, is relatively small, occupying 4.31% in D_1 and 2.95% in D_2 . In addition, there is no particular reason to believe that the last conversation partner in a day and the first partner in the next day are specifically correlated. In this study, we did not correct for the effect of the night and weekend.

The degree of predictability depends on individuals. In particular, we have shown that individuals connecting different communities in conversation networks behave relatively deterministically. We quantified the degree to which an individual is confined in communities by the clustering coefficient. In the context of overlapping community structure, individuals connect different communities when they belong to multiple overlapping communities [40]. Such individuals tend to be surrounded by many triangles if we define the community by 3-cliques (*i.e.*, triangles). This apparently contradicts our results. This contradiction comes from the difference in what we mean by connecting different communities. We regard individuals as bridging different communities when they are not strongly bound to any community and they have links to different communities. In this sense, nodes with small clustering coefficient values connect different communities in networks with hierarchal structure [42, 44]. In general, links bridging different communities have large betweenness centrality values [45]. The clustering coefficient of a node tends to decease with the betweenness centrality [46]. This lends another support to our view that individuals with small clustering coefficient values tend to connect different network communities. It should be noted that the "strength of weak ties" property of the CN and the relationship between I_i and the individuals' position in the CN are preserved, if we define the link weight by the total duration of the conversation events for each pair (see Appendix F).

We do not have an access to the contents of dialogs for ethics reasons. Therefore, the understanding of the reason for the correlation between the individual's position and predictability is limited. Nevertheless, individuals that own many weak links and connect distinct groups may mediate information flows necessary to coordinate tasks involving these groups (*e.g.*, project groups in a company). Such individuals may control the information flow between the groups in a rigid manner to yield a large I_i . In contrast, individuals with few weak links may enjoy casual (and perhaps creative) conversations within their own groups to choose the partners in a random manner. Such individuals may tend to have a small I_i . It should be noted that our data were obtained in company offices. Roles or formal positions of individuals in the company may affect I_i and the local abundance of weak links surrounding the individuals.

Song *et al.* discovered a remarkable predictability in the mobility patterns of humans [10]. In terms of the analysis tools, our methods are similar to theirs. We have applied the entropy measures and the concept of predictability to different types of data sets. In our data, the physical location of individuals is irrelevant; individuals work in offices in the companies. It should be noted that although we have not implemented the prediction algorithm, the predictability of the data is implied by the large mutual information that we observed. This logic parallels that made for human mobility patterns [10].

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Appendix

A. Results for data set D_2

We obtained qualitatively the same results for D_2 as those for D_1 . The results for D_2 are shown in Figs. A1, A2, A3, and A4, which correspond to Figs. 4, 5, 6, and 7 in the main text, respectively.

B. Details of the bootstrap test

To confirm that the large value of the empirically obtained I_i is not because of the small data size, we carry out a bootstrap test as follows. First, we make a bootstrap sample of a partner sequence with length s_i by resampling partners' IDs from the empirical partner sequence of individual i without replacement (*i.e.*, shuffling). Then, we use Eq. (4) to calculate the mutual information \hat{I}_i for the bootstrap sample. By resampling 5,000 bootstrap partner sequences, we construct the distribution of \hat{I}_i , which we denote as $p(\hat{I}_i)$. On the basis of $p(\hat{I}_i)$, we carry out a hypothesis test for I_i . The null hypothesis of the test is that I_i is positive just because of the small data size. The alternative hypothesis is that I_i is larger than the value expected for unstructured data of a small size. We set the significance level of the test to 1%. Consequently, the critical region of the null hypothesis is the half-open interval above the 99 percentile point of $p(\hat{I}_i)$. In Fig. A5, the results of the each error bar). In fact, for all the individuals in D_1 and D_2 , except individual 14 in D_1 and 149 in D_2 , the null hypothesis is rejected with a 1% significance level.

C. Long-tailed behavior of inter-event intervals

Human's activity patterns are characterized by long-tailed distributions of the inter-event intervals [1, 4–6, 8, 17–20], a feature that is shared by our data. We define the inter-event interval τ as the interval between the initiation time of two successive conversation events involving a given individual. The unit of τ is a minute, corresponding to the time resolution of the recording. As shown in Fig. A6(a), the distribution of τ , denoted by $p(\tau)$, for a typical individual in D_1 is long-tailed. The tail of the empirical data (solid line) is much fatter than that of the exponential distribution whose mean is equal to that of the empirical data (dashed line). The histogram of the coefficient of variation (CV) of $p(\tau)$ on the basis of all the individuals in D_1 and the same histogram for D_2 are shown in Fig. A6(b). The value of CV is equal to the ratio of the standard deviation to the mean and is equal to unity for exponential distribution. Figure A6(b) indicates that the CV of $p(\tau)$ is much larger than unity for all the individuals.

D. Components of the predictability of conversation events

A possible mechanism governing the predictability of the conversation events is the bursty activity patterns. To examine the effect of long-tailed behavior of $p(\tau)$ on the predictability, we carry out a statistical test based on the shuffling of I_i as follows. Consider the sequence of conversation events of focal individual i with individual j. If i and j talk four times in a given day and the inter-event intervals are equal to τ_1 , τ_2 , and τ_3 in the chronological order, we randomize their order. For example, the interevent intervals in the shuffled data are ordered as τ_2 , τ_1 , and τ_3 . We carry out the same randomization for each day and each partner j. Then, we combine the randomized sequences (*i.e.*, point processes) for different *i*s into one point process from which we read out the randomized partner sequence for i. We define I_i^{burst} as the mutual information for this randomized partner sequence. In Fig. 5(a), the mean and standard deviation of I_i^{burst} obtained from 100 randomized partner sequences are shown for different individuals in D_1 . The empirical values of I_i (circles) are significantly larger than I_i^{burst} for most individuals. However, I_i^{burst} consistently occupies a large fraction of I_i and increases with I_i . Therefore, the burstiness is a major cause of the predictability regardless of the value of I_i . The burstiness is not the only contributor to the predictability. To show this, we examine the reduced partner sequence generated by merging all the consecutive events with the same partner into one event. For example, the original partner sequence $\{2, 3, 3, 6, 4, 4, 3, 3, 3, 2, 6, 2\}$ yields the merged partner sequence $\{2, 3, 6, 4, 3, 2, 6, 2\}$. We calculate the mutual information in the merged partner sequence, denoted by I_i^{merge} . I_i^{merge} measures the predictability of conversation events that does not result from the burstiness. We do not directly compare I_i^{merge} with the original I_i because the merging procedure shortens the length of the partner sequence and the amount of mutual information generally depends on the length of a sequence. Instead, we carry out a bootstrap test for I_i^{merge} . By definition, the partner changes every time in the merged partner sequence. We obtain bootstrap samples respecting this property as follows. The frequency with which partner j appears in the merged partner sequence of individual j is denoted by $P_i^{\text{merge}}(j)$. We select the first partner of i, denoted by ℓ , randomly according to $P_i^{\text{merge}}(j)$. The second partner is selected according to $P_i^{\text{merge}}(j)/(1 - P_i^{\text{merge}}(\ell))$, where $j \neq \ell$. We repeat the same procedure until the generated sequence becomes as long as the merged partner sequence. Figure 5(b) summarizes the results of the bootstrap test for I_i^{merge} . I_i^{merge} is consistently larger than the values expected for the bootstrap samples for all the individuals. Therefore, the partner

sequence is predictable to some extent even without the effect of the bursty activity patterns.

E. Use of normalized mutual information

In the field of cluster partitioning, the normalized mutual information $\overline{I}_i \equiv I_i/H_i^1$ is used to quantify the accuracy of partitioning methods, because the relationship $0 \leq \overline{I}_i \leq 1$ is convenient for comparing different methods [37]. Our main results are qualitatively the same if we replace I_i by \overline{I}_i (Fig. A7).

F. Alternative definition of the link weight based on the duration of conversation

In the main text, we defined the link weight by the total number of the conversation events for each pair. An alternative definition is given by the total duration of the conversation events for each pair. This alternative definition changes w_{ij} , s_i , and \overline{w}_i and conserves k_i , $H_i^{0,1,2}$, and I_i . For the CN where the link weight is defined by the total duration, we repeat the same set of analysis as that conducted in Sec. 3.3. As shown in Fig. A8, the change in the definition of the link weight does not affect our main results. We observed a negative correlation between I_i and s_i (Fig. A8(a)), that between I_i and \overline{w}_i (Fig. A8(b)), the "strength of weak ties" property (Fig. A8(c)), and a negative correlation between I_i and $C_i(w_{\text{thr}})$ (Fig. A8(d)).

G. Robustness against observation failures

To examine the robustness of our results against observation failures, we analyze the data sets after interpolating short intervals between successive conversations between the same pairs of individuals. Suppose that individuals i and j talk with each other twice and that i does not talk with anybody else between the two conversation events with j. We merge the two conversation events into one if the difference between the ending time of the first event and the starting time of the second event is less than m minutes.

In Fig. A9, \tilde{s}_i , \tilde{H}_i^1 , \tilde{H}_i^2 , and \tilde{I}_i , which are the quantities calculated for the data obtained with m = 1, are compared with s_i , H_i^1 , H_i^2 , and I_i , respectively. As expected, \tilde{s}_i is smaller than s_i , and \tilde{H}_i^1 and \tilde{H}_i^2 are generally larger than H_i^1 and H_i^2 , respectively. As shown in Fig. A10, the important properties of the data sets are not changed by the interpolation with m = 1. In other words, a negative correlation between \tilde{I}_i and \tilde{s}_i (Fig. A10(a)) and that between \tilde{I}_i and \tilde{w}_i (Fig. A10(b)), the "strength of weak ties" property (Fig. A10(c)), and a negative correlation between \tilde{I}_i and $C_i(w_{\text{thr}})$ (Fig. A10(d)) are observed. The results are qualitatively the same for m = 5, as shown in Figs. A11 and A12.

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Figure 1: Procedure for generating the partner sequence of individual 1. (a) Original data set. (b) List of conversation events that involve individual 1. (c) Partner sequence of individual 1. The data set shown in (a) is an artificial one, for the purpose of explanation.



Figure 2: Visualization of CN G_1 . For clarity, only the nodes with strengths larger than 100 and the links among them are drawn. The darkness of the node color represents the value of I_i ; a darker node has a larger I_i . The thickness of the link is proportional to its weight. The links with weights larger than or equal to (smaller than) the median value (*i.e.*, 5) are drawn by red (blue) lines.



Figure 3: Cumulative distribution of (a) degree, (b) node strength, and (c) link weight of the CNs.



Figure 4: (a) Histograms of the entropies for D_1 . (b) Relationship between H_i^1 and H_i^2 in D_1 . The solid line represents $H_i^1 = H_i^2$.



Figure 5: Results of the bootstrap test for D_1 . The circles represent I_i and I_i^{merge} in (a) and (b), respectively. The error bars represent the statistics for the bootstrap samples. (a) Results of the shuffling test. I_i and the error bars are plotted in the ascending order of I_i . The error bars indicate one standard deviation around the mean of I_i^{burst} , obtained from 100 shuffled partner sequences. The ticks at the middle of the error bars indicate the mean. (b) Results of the merging test. I_i^{merge} and the confidential intervals (error bars) are plotted in the ascending order of I_i^{merge} . The lower and upper ends of the error bars represent 0 and 99 percentile points, respectively. The ticks at the middle of the mean.



Figure 6: Mutual information I_i is plotted against (a) degree k_i , (b) node strength s_i , and (c) average node weight \overline{w}_i , for D_1 . The Pearson correlation coefficient R between the plotted quantities is also shown.



Figure 7: (a) Averaged neighborhood overlap $\langle O \rangle_w$ as a function of the fraction of links with weights smaller than w for D_1 . (b) Pearson correlation coefficient between I_i and $C_i(w_{\text{thr}})$ (squares) and the partial correlation coefficient between them with $k_i(w_{\text{thr}})$ and $s_i(w_{\text{thr}})$ fixed (circles), for D_1 . The horizontal line represents zero correlation.



Figure A1: (a) Histograms of the entropies for D_2 . (b) Relationship between H_i^1 and H_i^2 in D_2 . The solid line represents $H_i^1 = H_i^2$.



Figure A2: Results of the bootstrap tests for D_2 on the basis of (a) shuffling and (b) merging of the partner sequence. See the caption of Fig. 5 for legends.



Figure A3: Mutual information I_i is plotted against (a) degree k_i , (b) node strength s_i , and (c) average node weight \overline{w}_i , for D_2 . The Pearson correlation coefficient R between the plotted quantities is also shown.



Figure A4: (a) Averaged neighborhood overlap $\langle O \rangle_w$ as a function of the fraction of links with weights smaller than w for D_2 . (b) Pearson correlation coefficient between I_i and $C_i(w_{\text{thr}})$ (squares) and the partial correlation coefficient between them with $k_i(w_{\text{thr}})$ and $s_i(w_{\text{thr}})$ fixed (circles), for D_2 .



Figure A5: Results of the bootstrap test of the finite size effect for (a) D_1 and (b) D_2 . I_i (circles) and the confidential intervals (error bars) of individuals are plotted in the ascending order of I_i . The lower and upper ends of the error bars represent 0 and 99 percentile points, respectively. The ticks at the middle of the error bars indicate the mean.



Figure A6: (a) Cumulative distribution of the inter-event intervals of a typical individual in D_1 (solid line). The dotted line represents the power-law fit with exponent -1.52, obtained from the maximum likelihood test [47]. The dashed line represents the exponential distribution with the same mean as that of the data. (b) Distributions of the CV of $p(\tau)$ in D_1 and D_2 .



Figure A7: Normalized mutual information \overline{I}_i is plotted against (a) degree k_i , (b) node strength s_i , and (c) average node weight \overline{w}_i , for D_1 . The Pearson correlation coefficient R between the plotted quantities is also shown. (d) Pearson correlation coefficient between \overline{I}_i and $C_i(w_{\text{thr}})$ (squares) and the partial correlation coefficient between them with $k_i(w_{\text{thr}})$ and $s_i(w_{\text{thr}})$ fixed (circles).



Figure A8: Results when the link weight is defined by the total duration of the conversation events for each pair, for D_1 . The mutual information I_i is plotted against (a) node strength s_i and (b) average node weight \overline{w}_i . The Pearson correlation coefficient R between the plotted quantities is also shown. (c) Averaged neighborhood overlap $\langle O \rangle_w$ as a function of the fraction of links with weights smaller than w. (d) Pearson correlation coefficient between I_i and $C_i(w_{\text{thr}})$ (squares) and the partial correlation coefficient between them with $k_i(w_{\text{thr}})$ and $s_i(w_{\text{thr}})$ fixed (circles).



Figure A9: Comparison between the interpolated and original data for data sets D_1 and D_2 . (a) Node strength, (b) uncorrelated entropy, (c) conditional entropy, and (d) mutual information for the interpolated data with m = 1 are plotted against those without interpolation (*i.e.*, original data sets).



Figure A10: Results for the interpolated data with m = 1. We use data set D_1 . The mutual information is plotted against (a) node strength and (b) mean weight. (c) Averaged neighborhood overlap $\langle O \rangle_w$ as a function of the fraction of links with weights smaller than w. (d) Pearson correlation coefficient (squares) and partial correlation coefficient (circles) between I_i and $C_i(w_{\text{thr}})$.



Figure A11: Comparison between the interpolated and original data for data sets D_1 and D_2 . (a) Node strength, (b) uncorrelated entropy, (c) conditional entropy, and (d) mutual information for the interpolated data with m = 5 are plotted against those without interpolation (*i.e.*, original data sets).



Figure A12: Results for the interpolated data with m = 5. We use data set D_1 . See the caption of Fig. A10 for legends.